

# Quantum Field Theory 2: the Standard Model

## Syllabus

The page numbers mentioned in this short course overview refer to the handwritten lecture notes. More extended information can be found on Brightspace in the weekly content sections.

### Lecture 1: page 1-7, Ex.1+2

- Summary of basic QFT concepts (scalar Lagrangians, Noether's theorem, etc.).
- QED from local  $U(1)$  gauge invariance (gauge principle, covariant derivative, field tensor, massless gauge field as force mediator, scalable Abelian gauge interactions, charge).

### Lecture 2: page 7-12, Ex.3+4

- Generalising the gauge principle to describe other fundamental forces in the SM.
- Non-Abelian local  $SU(N)$  invariance for  $N>1$  (Lie algebra, generators, matter fermions in fundamental representation, non-Abelian gauge bosons in adjoint representation, non-scalable non-Abelian interactions, triple and quartic self interactions among gauge bosons).

### Lecture 3: page 12-16, Ex.5

- Experimental evidence hinting at  $SU(3)_c$  ( $c$  = colour) for describing strong interactions and  $SU(2)_L$  ( $L$  = left-handed matter-fermion chirality) for describing weak interactions.
- The weak interactions require a chiral theory and massive gauge bosons!

### Lecture 4: page 16-20, Ex.6+7

- The SM gauge group is completed by adding the  $U(1)_Y$  ( $Y$  = hypercharge) gauge group.
- List of all SM matter fermions (leptons + quarks) and their gauge-group quantum numbers.
- Theoretical issue: in a chiral theory quantum corrections may invalidate the Ward identities that reflect gauge invariance (chiral anomaly), which would have disastrous consequences.

### Lecture 5: page 20-23, continuation of the week 4 exercise set

- The SM is “magically” anomaly free due to the lepton-quark family structure and the lepton and quark gauge quantum numbers.
- The issue of having massive weak gauge bosons and matter fermions in the SM.
- The concept of spontaneous symmetry breaking (Higgs mechanism) to remedy this: the physical Higgs boson and the fate/role of the Goldstone bosons.

### Lecture 6: page 24-27, Ex.8+9

- The SM Higgs mechanism for giving mass to the  $W$  and  $Z$  bosons and all massive fermions.
- Mixing of gauge eigenstates into mass eigenstates:  $SU(2)_L$  and  $U(1)_Y$  gauge bosons  $\rightarrow$  massive  $W^+$ ,  $W^-$ ,  $Z$  bosons and massless photon, and flavour mixing in the fermion sector (e.g. CKM quark-mixing matrix).

### Lecture 7: page 28-32, Ex.10

- Consequences of mixing in the quark and lepton sectors (GIM mechanism, neutrino oscillations, CP violation  $\Rightarrow$  at least three generations of matter fermions in the SM).

## Exercises:

- 1: Setting the scene for non-Abelian  $SU(N)$  and  $SO(N)$  gauge theories
- 2: Properties of a conjugate  $SU(2)$  doublet
- 3: Absence of scalability of non-Abelian interactions
- 4: Feynman rules for the  $SU(N)$  interactions (gauge interactions, TGC, QGC)
- 5: Propagator for a massive gauge boson and the ensuing problematic UV behaviour
- 6: Some covariant derivatives that feature in the Standard Model
- 7: The relativistic superconductor (a Higgs toy model inspired by the Meissner effect)
- 8: Gauge-boson masses in the Standard Model
- 9: Neutral-current and charged-current electroweak gauge interactions for quarks
- 10: Highlighting aspects of neutrino oscillations